## Two kinds of modified numerals

Class $\mathrm{A} / \mathrm{B}$ distinction (Nouwen, 2010): classification of modifiers into two categories: those that give rise to obligatory ignorance inferences (class $B$ ) and those that do not (class A)

## (1) Class A

I know exactly how many books I have, and it's \{ more than / fewer than under / over $\} 200$.
(2) Class B
\#| know exactly how many books I have, and it's \{at least / at most minimally / maximally / up to \} 200 .

## Upper-bounded numeral modifiers

## - Our focus: the bounds of numeral modifiers

- Up to behaves differently from other upper-bounded numeral modifiers

1. NPI licensing (Schwarz et al., 2012):
(3) a. $\{$ At most $/$ Fewer than $/ * U$ p to $\}$ five students have ever ben in this cave.
b. $\begin{aligned} & \text { At most / Fewer than / } \\ & \text { damn about Pavarotti. to }\} \text { three students give a }\end{aligned}$ damn about Pavarotti.
2. Cancellable upper bound (Blok, 2015):
(4) a. \#At most ten people died in the crash, perhaps even more. b. \#Fewer than ten people died in the crash, perhaps even more.
3. Non-cancellable lower bound (Blok, 2015):
(5) a. At most three students will show up to the lecture, if any. b. ? Fewer than three students will show up to the lecture if any c. \#Up to three students will show up to the lecture, if any.

Entailed and implicated upper bounds (Blok, 2015)

- Up to asserts a lower bound; at most and fewer than do not
- Up to implicates an upper bound; at most and fewer than assert an upper bound

|  | Lower bound |
| :--- | :--- |
| Upper bound |  |
| at most 10 | - |
| fewer than 10 | - |
| up | semantic |
| up to 10 | semantic |
| semantic |  |
| pragmatic |  |

(6) Up to ten people died in the crash.

- Semantics of (6): for every number on a scale [1...10], the speaker considers it possible that that many people died in the crash
- Implicature for (6): for every number in [11... $\infty$ ), the speaker does not consider it possible that that many people died in the crash
(7) \{At most ten / Fewer than eleven \} people died in the crash.
- Semantics of (7): MAX ${ }_{n}$ [(the speaker considers it possible that) $\boldsymbol{n}$ people died in the crash] $=10$

Additional evidence: interaction with evaluative predicates

- Evaluative adverbs target the assertion of an utterance rather than its implicature (Nouwen, 2006):
(8) a. Fortunately, some students attended the wedding.
b. Fortunately, the soup is warm.
- This also holds for up to, at most, and fewer than:
(9) a. Fortunately, up to 100 people will attend my wedding.
b. Fortunately, $\{$ at most / fewer than \} 100 people will attend my
wedding. wedding.
- Related notion: directivity (Nouwen, 2010b): certain quantifiers (such as up to n) highlight the elements for which the predicate holds, while others (such as at most / fewer than n ) highlight the elements for which the predicate does not hold
- Another factor: granularity/distance (Cummins, Sauerland, and Solt 2012):
(11) John's birthplace has more than 1000 inhabitants.
$\nrightarrow$ John's birthplace doesn't have more than 1001 inhabitants.

$$
\rightarrow \text { John's birthplace doesn't have more than a million inhabitants. }
$$

$\rightarrow$ John's birthplace doesn't have more than a million inhabitants.

## Research questions

- Is it the case that the upper bound of up to is cancellable (which would support an implicature-based account)?
- If so, to what extent?
(experiment $1 \& 2$ )
- Does distance play a role? (experiment 2)

$$
\begin{aligned}
& \text { (10) a. In the airplane crash, \{few / not quite all / at most ten / fewer } \\
& \text { than ten\} passengers were killed, which is a good thing. } \\
& \text { b. ?In the airplane crash, a few a almost all up to ten\}. } \\
& \text { passengers were killed, which is a good thing. }
\end{aligned}
$$

## The role of distance in implicature calculation

(ex 2)


## - 1st sentence:

$\triangleright$ Naturally occurring sentences adapted from HNC
$\triangleright n$ : almost exclusively non-round numbers

- 2nd sentence:
$\triangleright$ Statement about a specific instance
$\triangleright \boldsymbol{m}$ (discrepancy conditions):
- $\boldsymbol{m}<\boldsymbol{n}$ 'under'
- $\boldsymbol{m}>\boldsymbol{n}$ 'over
$\triangleright$ Small distance between $\boldsymbol{m}$ and $\boldsymbol{n}$


## Methods (b)

- Numeral modifier x Discrepancy
- Control: fewer than: asserted upper bound (Hackl 2000; Nouwen, 2010)
- 12 items, rotated through (6) lists
- 14 fillers ( 7 coherent discourses \& 7 contradictory discourses)
- 143 native speakers of Greek* ( 98 female participants, 2 no gender info; mean age: 32.8; age range: 19-67)
- Filled in on-line (created on uvw. surveymonkey. com)



## Conclusions

## 'Under' condition: Conclusion

- In a natural discourse setting (Exp. I)
$\square$ Lower rates in the 'under' condition for up to
$\triangleright$ Possibly associated with directivity: quantifiers with positive directivity like up to trigger the expectation that higher numbers should be used in subsequent discourse


## Experiment II

- Follow-up in English
- Numeral modifiers: fewer/ less than, at most, up to
- Modifications:
$\triangleright$ Fine granularity: $\boldsymbol{n}$ : clearly non-round number
$\triangleright$ Control for $\boldsymbol{m}$ vs. $\boldsymbol{n}$ distance
$\triangleright$ Avoid interpretation of 'over' items as exceptions $\rightarrow$ Different task


## Methods (a)

- Compatibility judgement task

CLAIM: Clarendon High School used its smart classrooms 50 times last year
(fewer than //) with $\left\{\begin{array}{c}\text { fewer than/ } \\ \text { less than }\end{array}\right)$
with $\left.\begin{array}{c}\text { less than } \\ \text { at most } \\ \text { up to }\end{array}\right\} \boldsymbol{n}$ students participating in this classroom environment.
FACT: On one occasion the smart classroom was used at Clarendon High School last year, $\boldsymbol{m}$ students participated.

How compatible is the CLAIM with the FACT? $\begin{array}{lllllll}-3 & -2 & -1 & 0 & 1 & 2 & 3\end{array}$
$\begin{array}{cc}\text { completely } \\ \text { incompatible } & \begin{array}{c}\text { completely } \\ \text { compatible }\end{array}\end{array}$

## - Claim:

$\triangleright$ Claims with up to $\boldsymbol{n}$ drawn from COCA (Davies, 2008)
$\triangleright n$ : clear cases of non-round numbers

- Fact:
$\triangleright$ Highlights a specific instance
$\triangleright \boldsymbol{m}$ (discrepancy conditions):
$\boldsymbol{m}=\boldsymbol{n} * 0.95$ 'under'
$\boldsymbol{m}=\boldsymbol{n} * 0.25$ 'way under'
$m=n * 1.05$ 'over'
- m=n*1.75'way over'


## Methods (b)

- Numeral modifier x Discrepancy
- Target items ( $\mathrm{N}=28$ ) rotated through lists
- 30 filler items with quantifiers ( 10 contradictions, 10 entailments, 10 implicatures)
- 45 participants on Amazon's Mechanical Turk (31 female participants; mean age: 38.98; age range: 21-59)

Results


- 'Over' condition: Significantly higher scores for up to than for fewer than and at most $(\beta=.7879, S E=.1756, p<.01$ and $\beta=.639, S E=.17, p<.01$, respectively)
- 'Way over' condition: Higher scores for up to than for fewer than (significantly) and at most (marginally) $(\beta=.41, S E=.176, p<.05$ and $\beta=.348, S E=.19, p=.07$, respectively)
- Scores for 'over' significantly higher than for 'way over' for each modifier, with the smallest effect for fewer than ( $\beta=.69, S E=.170, p<.01$ vs. $\beta=.842, S E=.192$, $p<0.01$ for at most and $\beta=.824, S E=.164, p<0.01$ for up to)
- 'Under' and 'way under' conditions: No differences between the modifiers and within each modifier ( $\boldsymbol{p}>.1$ )
- No significant difference between fewer than and at most ( $\boldsymbol{\rho}>.1$ )


## 'Over' conditions: Overall conclusions

- The upper-bound construal of
$\triangleright$ up to is pragmatically derived
$\triangle$ at most is part of its lexical semantics
in favour of Blok (2015)
Distance affects the degree to which the upper-bound construal is drawn


## - Effect of distance

$\triangleright$ Scalar/semantic distance - similar findings for other scalar terms (Beltrama and Xiang, 2013; van Tiel et al., 2014): e.g., many/some $\leadsto$ not all $>$ many/some $\leadsto$ not most
$\triangleright$ Distance in rates may be mapped onto actual numeric distance $\rightarrow$ Effect for all numeral modifiers
$\triangleright$ Extreme values ruled out by Relevance $\rightarrow$ Effect for all numeral modifiers

- Likert scale (vs. binary judgment task): Good metric for semantic $\neq$ pragmatic inferences (Cummins \& Katsos, 2010; Hansen \& Chemla, 2013)
$\triangleright$ Choice of the particular Likert scale is irrelevant (contra Cummins \& Katsos, 2010)
$\triangleright$ Criterion: Difference from contradictions (here: difference from control items with fewer than in the 'over' condition)
$\triangleright$ Greater range of ratings also a criterion (variation among speakers)?

