

# The extent of upper-bound construals among different modified numerals

Stavroula Alexandropoulou

Yaron McNabb

Sofia Bimpikou

Dominique Blok

Rick Nouwen

Universiteit Utrecht

MXPRAG

June 2 2015

# Inferences and modified numerals

- ▶ Modified numerals give rise to wide variety of inferences
- ▶ Example 1: variation inferences (Nouwen, 2015)

(1) The CNN crew got that bit of video, and everyone in the world has seen it at least twenty times.  
→ there is no specific  $n$  such that everyone has seen the video  $n$  many times

# Inferences and modified numerals

- ▶ Modified numerals give rise to wide variety of inferences
- ▶ Example 1: variation inferences (Nouwen, 2015)

(1) The CNN crew got that bit of video, and everyone in the world has seen it at least twenty times.

→ there is no specific  $n$  such that everyone has seen the video  $n$  many times

(2) A: According to a random sample every bag contains at least 22 sweets.

B: ?Do they all contain the same number of sweets?

Alexandropoulou (to appear)

# Inferences and modified numerals

- ▶ Example 2: scalar inferences (Krifka, 1999; Fox and Hackl, 2006)

(3) John has three children.  
→ John doesn't have four children.

# Inferences and modified numerals

- ▶ Example 2: scalar inferences (Krifka, 1999; Fox and Hackl, 2006)

(3) John has three children.

→ John doesn't have four children.

(4) John has more than three children.

↯ John doesn't have more than four children

# Inferences and modified numerals

- ▶ Example 2: scalar inferences (Krifka, 1999; Fox and Hackl, 2006)

(3) John has three children.

→ John doesn't have four children.

(4) John has more than three children.

↯ John doesn't have more than four children

(5) I can say with certainty that John has more than three children.

→ I cannot say with certainty that John has more than four children

# Inferences and modified numerals

- ▶ Another factor: granularity/distance (Cummins et al., 2012)
  - (6) John's birthplace has more than 1000 inhabitants.
    - ↗ John's birthplace doesn't have more than 1001 inhabitants.
    - John's birthplace doesn't have more than a million inhabitants.

# Inferences and modified numerals

- ▶ Not all modified numerals give rise to the same kinds of inferences
- ▶ Class A/B distinction (Nouwen, 2010a): class B numeral modifiers give rise to obligatory ignorance inferences



# Inferences and modified numerals

- ▶ Not all modified numerals give rise to the same kinds of inferences
- ▶ Class A/B distinction (Nouwen, 2010a): class B numeral modifiers give rise to obligatory ignorance inferences

(7) **Class A**

I know exactly how much memory my laptop has, and it's { more than / less than / under / over } 4GB.

(8) **Class B**

#I know exactly how much memory my laptop has, and it's { at least / at most / minimally / maximally / up to } 4GB.

# The bounds of modified numerals

- ▶ Focus of our study: differences among class B modifiers

# The bounds of modified numerals

- ▶ Focus of our study: differences among class B modifiers
- ▶ NPI licensing data suggest that *up to* is different from other class B modifiers that set an upper bound (Schwarz, Buccola, & Hamilton, 2012):

(9) { At most / \*up to } five students have ever been in this cave.

(10) { At most / \*up to } three students give a damn about Pavarotti.

# The bounds of modified numerals

- ▶ Focus of our study: differences among class B modifiers
- ▶ NPI licensing data suggest that *up to* is different from other class B modifiers that set an upper bound (Schwarz, Buccola, & Hamilton, 2012):

(9) { At most / \*up to } five students have ever been in this cave.

(10) { At most / \*up to } three students give a damn about Pavarotti.

- ▶ This suggests *at most* is downward monotone, which is expected given the fact that it sets an upper bound
- ▶ What about *up to*?

# The bounds of modified numerals

- ▶ Blok (SALT 2015): Schwarz et al.'s findings extend to directional numeral modifiers crosslinguistically

(11) Greek: **mehri**

- Perpatisame mehri tin akri tis limnis.  
We walked MEHRI the edge of the lake.  
'We walked up to the edge of the lake.'
- Ston anelkistira khorane mehri 5 atoma.  
In the elevator fit MEHRI 5 people.  
'Up to 5 people can fit in the elevator.'

# The bounds of modified numerals

- ▶ Blok (2015): there are two additional differences between directional numeral modifiers and expressions like *at most*:
  1. Directional numeral modifiers have a cancellable upper bound
  2. Directional numeral modifiers set a non-cancellable lower bound

# The bounds of modified numerals

- ▶ The upper bound of directional numeral modifiers can be cancelled:

- (12)
- #At most ten people died in the crash, perhaps even more.
  - Up to ten people died in the crash, perhaps even more.
- (13)
- #Leftovers keep in the refrigerator for at most one week or more.
  - Leftovers keep in the refrigerator for up to one week or more.

# The bounds of modified numerals

- ▶ The lower bound of directional numeral modifiers cannot be cancelled:
  - (14) a. At most three students will show up to the lecture, if any.
  - b. #Up to three students will show up to the lecture, if any.



# The bounds of modified numerals

Summary of the data:

- ▶ Directional numeral modifiers do not license NPIs; expressions like *at most* do

# The bounds of modified numerals

Summary of the data:

- ▶ Directional numeral modifiers do not license NPIs; expressions like *at most* do
- ▶ Directional numeral modifiers have a cancellable upper bound; expressions like *at most* have a non-cancellable upper bound

# The bounds of modified numerals

Summary of the data:

- ▶ Directional numeral modifiers do not license NPIs; expressions like *at most* do
- ▶ Directional numeral modifiers have a cancellable upper bound; expressions like *at most* have a non-cancellable upper bound
- ▶ Directional numeral modifiers have a non-cancellable lower bound; expressions like *at most* do not

# An implicature-based account

Central proposal (Blok, SALT 2015):

- ▶ Directional numeral modifiers assert a lower bound
- ▶ Directional numeral modifiers only implicate an upper bound

## An implicature-based account

- ▶ Directional numeral modifiers convey that the degree predicate they combine with holds for an interval on a scale
- ▶ Directional numeral modifiers assert a lower bound: the lowest number on the scale it quantifies over cannot be 0
- ▶ There is no maximality operator or other mechanism that sets an upper bound in the semantics

## An implicature-based account

- ▶ Directional numeral modifiers convey that the degree predicate they combine with holds for an interval on a scale
- ▶ Directional numeral modifiers assert a lower bound: the lowest number on the scale it quantifies over cannot be 0
- ▶ There is no maximality operator or other mechanism that sets an upper bound in the semantics
- ▶ (15) conveys that for every number on a scale  $[1\dots 10]$ , the speaker considers it possible that that many people died in the crash — without excluding any other possibilities

(15) Up to ten people died in the crash.

# An implicature-based account

How can this account for the data?

- ▶ As directional numeral modifiers assert a lower bound and implicate an upper bound, the cancellation facts follow straightforwardly from the account

# An implicature-based account

How can this account for the data?

- ▶ As directional numeral modifiers assert a lower bound and implicate an upper bound, the cancellation facts follow straightforwardly from the account
- ▶ The fact that directional numeral modifiers are upward entailing is compatible with the fact that they do not license NPIs



# An implicature-based account

Additional evidence: the interaction with evaluative adverbs

- ▶ Evaluative adverbs target the assertion of an utterance rather than its implicature (Nouwen, 2006)

- (16)
- Fortunately, some students attended the wedding.
  - Fortunately, the soup is warm.

# An implicature-based account

Additional evidence: the interaction with evaluative adverbs

- ▶ Evaluative adverbs target the assertion of an utterance rather than its implicature (Nouwen, 2006)

- (16)
- a. Fortunately, some students attended the wedding.
  - b. Fortunately, the soup is warm.

- ▶ This also holds for *up to* and *at most*

- (17)
- a. Fortunately, up to 100 people will attend my wedding.
  - b. Fortunately, at most 100 people will attend my wedding.

# An implicature-based account

Related notion: *directivity* (Nouwen, 2010b)

- (18) a. In the airplane crash, {few / not quite all / at most ten} passengers were killed, which is a good thing.
- b. ?In the airplane crash, {a few / almost all / up to ten} passengers were killed, which is a good thing.

# An implicature-based account

Related notion: *directivity* (Nouwen, 2010*b*)

- (18) a. In the airplane crash, {few / not quite all / at most ten} passengers were killed, which is a good thing.  
b. ?In the airplane crash, {a few / almost all / up to ten} passengers were killed, which is a good thing.
- (19) [In a commercial]  
a. Get a discount of up to 50%!  
b. ?Get a discount of at most 50%!

# Questions

Research questions:

- ▶ Is it the case that the upper bound of directional numeral modifiers is cancellable, which would support an implicature-based account?

# Questions

Research questions:

- ▶ Is it the case that the upper bound of directional numeral modifiers is cancellable, which would support an implicature-based account?
- ▶ Is there a contrast between where the lower bound of expressions like *at most* and directional numeral modifiers start?

# Questions

Research questions:

- ▶ Is it the case that the upper bound of directional numeral modifiers is cancellable, which would support an implicature-based account?
- ▶ Is there a contrast between where the lower bound of expressions like *at most* and directional numeral modifiers start?
- ▶ Does distance play a role?

# Questions

Research questions:

- ▶ Is it the case that the upper bound of directional numeral modifiers is cancellable, which would support an implicature-based account? (experiment 1 & 2)
- ▶ Is there a contrast between where the lower bound of expressions like *at most* and directional numeral modifiers start?
- ▶ Does distance play a role?



# Questions

## Research questions:

- ▶ Is it the case that the upper bound of directional numeral modifiers is cancellable, which would support an implicature-based account? (experiment 1 & 2)
- ▶ Is there a contrast between where the lower bound of expressions like *at most* and directional numeral modifiers start?
- ▶ Does distance play a role? (experiment 2)

# Questions

Research questions:

- ▶ Is it the case that the upper bound of directional numeral modifiers is cancellable, which would support an implicature-based account? (experiment 1 & 2)
- ▶ Is there a contrast between where the lower bound of expressions like *at most* and directional numeral modifiers start?  
(future research)
- ▶ Does distance play a role?  
(experiment 2)

# Experiments

- ▶ Compare **at most** vs. **up to**: cancellable upper bound
- ▶ Control: **fewer than**: asserted upper bound (Hackl, 2000; Nouwen, 2010a)

# Outline

Inferences and modified numerals

The bounds of modified numerals

An implicature-based account

Questions

**Experiments**

**Experiment 1**

Experiment 2

General discussion

Appendix

# Experiment 1

- ▶ Greek
- ▶ NMs:
  - ▶ *lighoteros/-i/-o' apo*, adj, 'fewer than' / *lighotero apo*, adv., 'less than'
  - ▶ *to poli*, *lit.* the much, 'at most'
  - ▶ *mehri*: DNM, also used in spatial & temporal domains

# Experiment 1

## Coherence judgement task

# Experiment 1

## Coherence judgement task

Interns in advertisement companies get  $\left\{ \begin{array}{l} \textit{less than} \\ \textit{at most} \\ \textit{up to} \end{array} \right\} n$  dollars per month; the interns in some of them are paid  $m$  dollars per month.

Is the underlined sentence a good continuation of the first sentence?

-3	-2	-1	0	1	2	3
very						very
bad						good

# Experiment 1

## Coherence judgement task

Interns in advertisement companies get  $\left\{ \begin{array}{l} \textit{less than} \\ \textit{at most} \\ \textit{up to} \end{array} \right\} n$  dollars per month; the interns in some of them are paid  $m$  dollars per month.

Is the underlined sentence a good continuation of the first sentence?

-3	-2	-1	0	1	2	3
very						very
bad						good

- ▶ 1st sentence:
  - ▶ Naturally occurring sentences adapted from *HNC (Hellenic National Corpus)* (2009)
  - ▶  $n$ : No real round number



# Experiment 1

## Coherence judgement task

Interns in advertisement companies get  $\left\{ \begin{array}{l} \textit{less than} \\ \textit{at most} \\ \textit{up to} \end{array} \right\} n$  dollars per month; the interns in some of them are paid  $m$  dollars per month.

Is the underlined sentence a good continuation of the first sentence?

-3	-2	-1	0	1	2	3
very						very
bad						good

- ▶ 2nd sentence:
  - ▶ Claim about a subset which is compatible or incompatible with the assertion in the 1st sentence
  - ▶  $m$ :  $m < n$  ('under') or  $m > n$  ('over') ( $m$  close to  $n$ )

# Experiment 1

## Methods

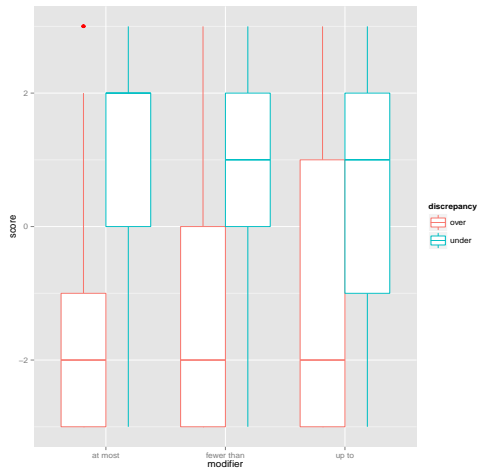
- ▶ Modifier (*lighotero(s) apo* 'less than/fewer than', *to poli* 'at most', *mehri* 'up to') × Discrepancy ( $m < n$  'under',  $m > n$  'over')
- ▶ 12 items, rotated through 6 lists
- ▶ 14 fillers (7 coherent discourses & 7 contradictory discourses), all appearing in every list
- ▶ 143 native speakers of Greek\*
- ▶ Filled in on-line (created on [www.surveymonkey.com](http://www.surveymonkey.com))

---

\*98 Female, 2 no gender info; Mean age: 32.8; Age range: 19–67

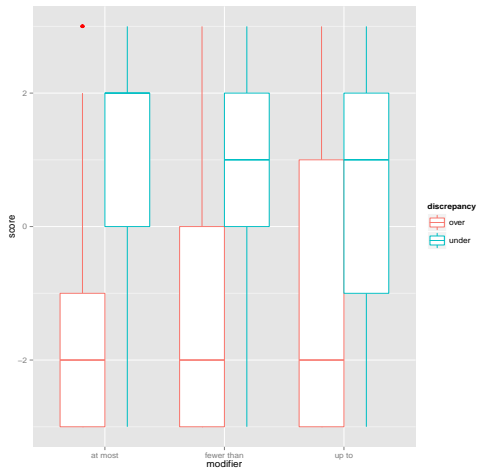
# Experiment 1

## Results



# Experiment 1

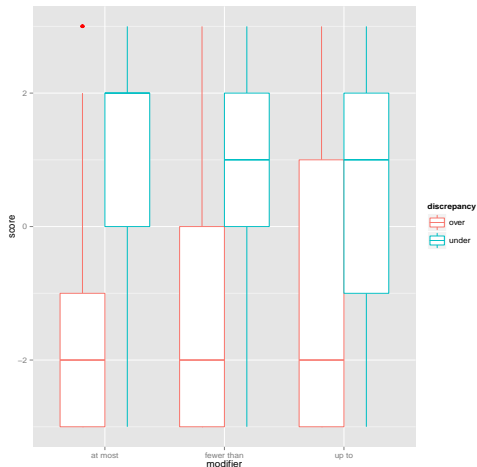
## Results



- ▶ 'Over' condition: Significantly higher coherence rates for **up to** than for **fewer than** and **at most** ( $\beta = .188$ ,  $SE = .089$ ,  $p < .05$  and  $\beta = .277$ ,  $SE = .09$ ,  $p < .01$ , respectively)

# Experiment 1

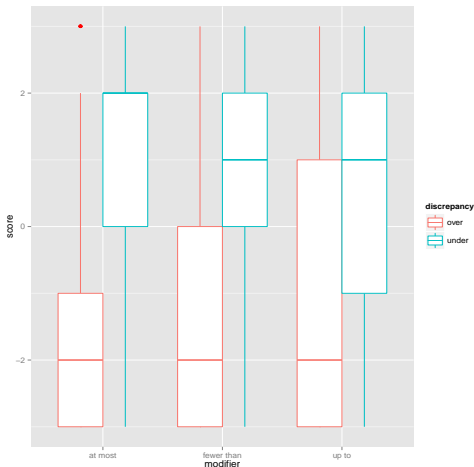
## Results



- ▶ 'Over' condition: Significantly higher coherence rates for **up to** than for **fewer than** and **at most** ( $\beta = .188$ ,  $SE = .089$ ,  $p < .05$  and  $\beta = .277$ ,  $SE = .09$ ,  $p < .01$ , respectively)
- ▶ 'Under' condition: Significantly lower coherence rates for **up to** than for **fewer than** and **at most** ( $\beta = -.215$ ,  $SE = .088$ ,  $p < .05$  and  $\beta = -.266$ ,  $SE = .088$ ,  $p < .001$ , respectively)

# Experiment 1

## Results



- ▶ 'Over' condition: Significantly higher coherence rates for **up to** than for **fewer than** and **at most** ( $\beta = .188$ ,  $SE = .089$ ,  $p < .05$  and  $\beta = .277$ ,  $SE = .09$ ,  $p < .01$ , respectively)
- ▶ 'Under' condition: Significantly lower coherence rates for **up to** than for **fewer than** and **at most** ( $\beta = -.215$ ,  $SE = .088$ ,  $p < .05$  and  $\beta = -.266$ ,  $SE = .088$ ,  $p < .001$ , respectively)
- ▶ No difference between **fewer than** and **at most** ( $p > .05$ )

# Experiment 1

## Conclusions

- ▶ Differences in 'over' condition:
  - ▶ The upper bound of **up to** in Greek is pragmatically derived (Note also: wider range of scores) → in favour of Blok's (2015) account
  - ▶ The upper bound of **at most** in Greek is part of its lexical semantics → in favour of Blok (2015)

# Experiment 1

## Conclusions

- ▶ Differences in 'over' condition:
  - ▶ The upper bound of **up to** in Greek is pragmatically derived (Note also: wider range of scores) → in favour of Blok's (2015) account
  - ▶ The upper bound of **at most** in Greek is part of its lexical semantics → in favour of Blok (2015)
- ▶ Differences in 'under' condition:
  - ▶ **Up to** associated with directivity:  $m < n$  → less felicitous

*Interns in advertisement companies get up to 980 dollars per month; the interns in some of them are paid 950 dollars per month.*



# Outline

Inferences and modified numerals

The bounds of modified numerals

An implicature-based account

Questions

## Experiments

Experiment 1

**Experiment 2**

General discussion

Appendix

## Experiment 2

- ▶ English
- ▶ Utterances with **up to Num** drawn from COCA Davies (2008)

## Modifications in Experiment 2

- ▶ 2nd sentences as exceptions in discourse setting → different task
- ▶ Control for granularity: clearly non-round numbers
- ▶  $m$  close to  $n$  → distance between  $m$  and  $n$  manipulated

## Example stimulus

CLAIM: Clarendon High School used its smart classrooms 50 times last year with  $\left\{ \begin{array}{c} \textit{fewer than} \\ \textit{at most} \\ \textit{up to} \end{array} \right\}$  39 students participating in this classroom environment.

FACT: On one occasion, the smart classroom was used at Clarendon High School last year,  $\left\{ \begin{array}{c} 10 \\ 37 \\ 41 \\ 68 \end{array} \right\}$  students participated.

How compatible is the CLAIM with the FACT?

-3  
completely  
incompatible

-2

-1

0

1

2

3

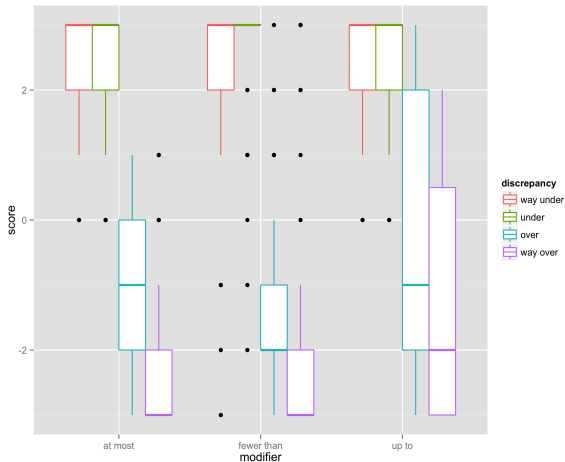
completely  
compatible

# Experimental design

- ▶ Numeral modifier factor: fewer than / at most / up to
- ▶ ( $n_{claim}$ ) vs. ( $m_{fact}$ ) discrepancy conditions:
  - ▶ under ( $m_{fact} < n_{claim}$ ):
    - ▶ under ( $m_{fact} = n_{claim} * 0.95$ )
    - ▶ way under ( $m_{fact} = n_{claim} * 0.25$ )
  - ▶ over ( $m_{fact} > n_{claim}$ ):
    - ▶ over ( $m_{fact} = n_{claim} * 1.05$ )
    - ▶ way over ( $m_{fact} = n_{claim} * 1.75$ )
- ▶ Target items (N=28) rotated through lists
- ▶ 30 filler items with quantifiers (10 contradictions, 10 entailments, 10 implicatures)
- ▶ 45 participants on Amazon's Mechanical Turk

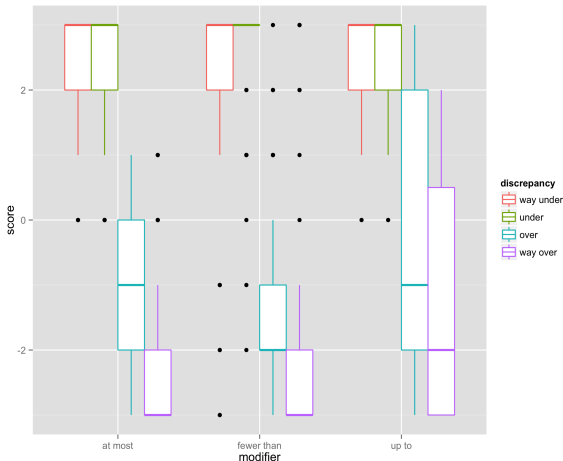
# Results

## Differences between modifiers



# Results

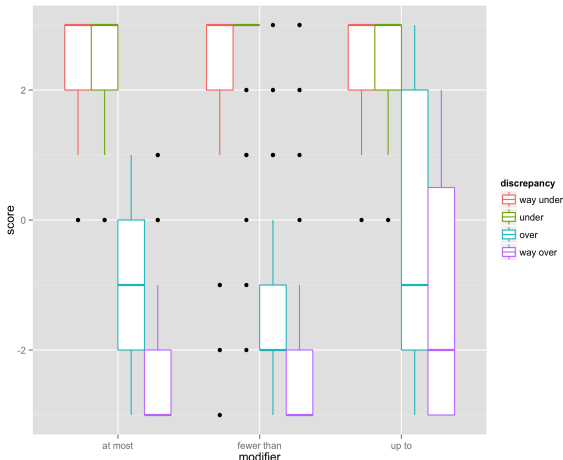
## Differences between modifiers



- 'Over' condition: Significantly higher coherence rates for **up to** than for **fewer than** and **at most** ( $\beta = .7879$ ,  $SE = .1756$ ,  $p < .01$  and  $\beta = .639$ ,  $SE = .17$ ,  $p < .01$ , respectively)

# Results

## Differences between modifiers



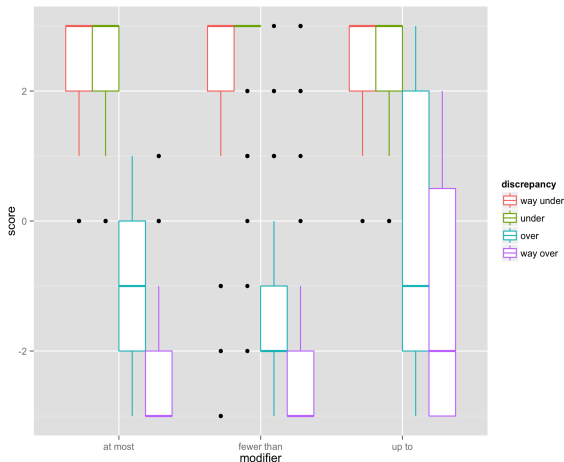
- ▶ 'Over' condition: Significantly higher coherence rates for **up to** than for **fewer than** and **at most** ( $\beta = .7879$ ,  $SE = .1756$ ,  $p < .01$  and  $\beta = .639$ ,  $SE = .17$ ,  $p < .01$ , respectively)

- ▶ 'Way over' condition: Higher coherence rates for **up to** than for **fewer than** (significantly) and **at most** (marginally) ( $\beta = .41$ ,  $SE = .176$ ,  $p < .05$  and  $\beta = .348$ ,  $SE = .19$ ,  $p = .07$ , respectively)



# Results

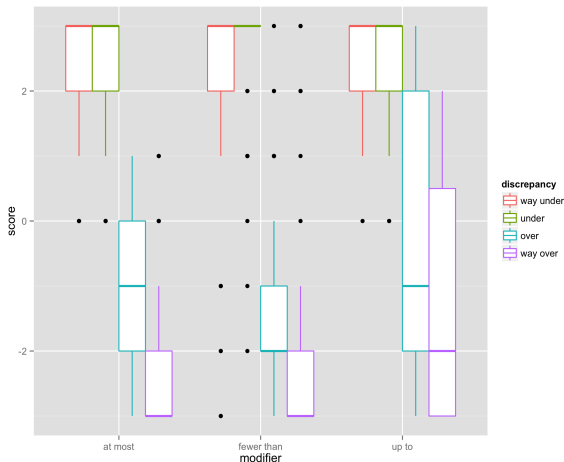
## Distance



- ▶ Rate for 'over' sig. higher than for 'way over' for each modifier, with the smallest effect for **fewer than** ( $\beta = .69$ ,  $SE = .170$ ,  $p < .01$  vs.  $\beta = .842$ ,  $SE = .192$ ,  $p < 0.01$  for **at most** and  $\beta = .824$ ,  $SE = .164$ ,  $p < 0.01$  for **up to**)

# Results

## Distance



- ▶ Rate for 'over' sig. higher than for 'way over' for each modifier, with the smallest effect for **fewer than** ( $\beta = .69$ ,  $SE = .170$ ,  $p < .01$  vs.  $\beta = .842$ ,  $SE = .192$ ,  $p < 0.01$  for **at most** and  $\beta = .824$ ,  $SE = .164$ ,  $p < 0.01$  for **up to**)
- ▶ 'Under' and 'way under' conditions: no differences between the modifiers and within each modifier

# Conclusions

- ▶ Differences in 'over' and 'way over' conditions:
  - ▶ Blok (2015): **at most** provides an upper-bound entailment
  - ▶ Blok: **up to**'s upper bound is pragmatically-derived
    - **over & way over** conditions: **up to** better than **at most** and **fewer than**
- ▶ Differences wrt Distance:
  - ▶ Distance affects the upper bound construal

# General findings

- ▶ Semantic vs. pragmatic upper bound in two different tasks →  
In favor of Blok's pragmatic account
- ▶ Distance affects upper bound construal (Experiment 2)
- ▶ **Up to** associated with directivity, thus less compatible with a follow-up focussing on a subset (Experiment 1)

# Up for discussion

- ▶ Effect of distance
  - ▶ Scalar/semantic distance – similar findings for other scalar terms (Beltrama and Xiang, 2013; Van Tiel et al., 2014): e.g., many/some  $\rightsquigarrow$  not all  $>$  many/some  $\rightsquigarrow$  not most

# Up for discussion

- ▶ Effect of distance
  - ▶ Scalar/semantic distance – similar findings for other scalar terms (Beltrama and Xiang, 2013; Van Tiel et al., 2014): e.g., many/some  $\rightsquigarrow$  not all  $>$  many/some  $\rightsquigarrow$  not most
  - ▶ Distance in coherence rates may be mapped onto actual numeric distance  $\rightarrow$  Effect in all MNs

# Up for discussion

- ▶ Effect of distance
  - ▶ Scalar/semantic distance – similar findings for other scalar terms (Beltrama and Xiang, 2013; Van Tiel et al., 2014): e.g., many/some  $\rightsquigarrow$  not all  $>$  many/some  $\rightsquigarrow$  not most
  - ▶ Distance in coherence rates may be mapped onto actual numeric distance  $\rightarrow$  Effect in all MNs
- ▶ Likert scale (vs. binary JT)  $\rightarrow$  semantic  $\neq$  pragmatic inferences (Cummins and Katsos, 2010; Katsos and Bishop, 2011)
  - ▶ A good metric?

# Up for discussion

- ▶ Effect of distance
  - ▶ Scalar/semantic distance – similar findings for other scalar terms (Beltrama and Xiang, 2013; Van Tiel et al., 2014): e.g., many/some  $\rightsquigarrow$  not all  $>$  many/some  $\rightsquigarrow$  not most
  - ▶ Distance in coherence rates may be mapped onto actual numeric distance  $\rightarrow$  Effect in all MNs
- ▶ Likert scale (vs. binary JT)  $\rightarrow$  semantic  $\neq$  pragmatic inferences (Cummins and Katsos, 2010; Katsos and Bishop, 2011)
  - ▶ A good metric?
  - ▶ If so, greater range of ratings also a criterion (variation among speakers)?



# Up for discussion

- ▶ Effect of distance
  - ▶ Scalar/semantic distance – similar findings for other scalar terms (Beltrama and Xiang, 2013; Van Tiel et al., 2014): e.g., many/some  $\rightsquigarrow$  not all  $>$  many/some  $\rightsquigarrow$  not most
  - ▶ Distance in coherence rates may be mapped onto actual numeric distance  $\rightarrow$  Effect in all MNs
- ▶ Likert scale (vs. binary JT)  $\rightarrow$  semantic  $\neq$  pragmatic inferences (Cummins and Katsos, 2010; Katsos and Bishop, 2011)
  - ▶ A good metric?
  - ▶ If so, greater range of ratings also a criterion (variation among speakers)?
- ▶ No difference between **at most** and **fewer than** – semantic identity or failure to find a difference?

Other points?

Thank you!

# Bibliography I

- Alexandropoulou, S. (to appear), Testing the nature of variability effects with modified numerals, in 'Paper presented at Sinn und Bedeutung (SuB) 19. Georg-August-Universität Göttingen'.
- Beltrama, Andrea and Ming Xiang (2013), Is good better than excellent? an experimental investigation on scalar implicatures and gradable adjectives, in E.Chemla, V.Homer and G.Winterstein, eds, 'Sinn und Bedeutung 17', pp. 81–98.
- Blok, D. (2015), 'The semantics and pragmatics of directional numeral modifiers', Unpublished draft, available at:  
<http://www.dominiqueblok.org/work>.
- Blok, Dominique (2015), The semantics and pragmatics of directional numeral modifiers. SALT.
- Cummins, C, Uli Sauerland and Stephanie Solt (2012), 'Granularity and scalar implicature in numerical expressions', *Linguistics & Philosophy* **35**, 135–169.
- Cummins, Chris and Napoleon Katsos (2010), 'Comparative and superlative quantifiers: Pragmatic effects of comparison type', *Journal of Semantics* **27**(3), 271 –305.
- Davies, Mark (2008), 'The corpus of contemporary american english: 425 million words, 1990-present'.

## Bibliography II

- Fox, Danny and Martin Hackl (2006), 'The universal density of measurement', *Linguistics and Philosophy* **29**(5), 537–586.
- Hackl, Martin (2000), Comparative Quantifiers, PhD thesis, MIT.
- HNC (Hellenic National Corpus)* (2009), Institute for Language and Speech Processing.  
**URL:** <http://hnc.ilsp.gr/en/default.asp>
- Katsos, Napoleon and Dorothy VM Bishop (2011), 'Pragmatic tolerance: Implications for the acquisition of informativeness and implicature', *Cognition* **120**(1), 67–81.
- Krifka, Manfred (1999), At least some determiners aren't determiners, *in* K. Turner, ed., 'The Semantics/Pragmatics Interface from different points of view', Elsevier Science, Oxford, pp. 257–291.
- Nouwen, Rick (2006), Remarks on the polar orientation of almost, *in* J. van de Weijer and B. Los, eds, 'Linguistics in the Netherlands', AvT publications 23, Benjamins.
- Nouwen, Rick (2010a), 'Two kinds of modified numerals', *Semantics and Pragmatics* **3**, 1–41.

## Bibliography III

- Nouwen, Rick (2010*b*), What's in a Quantifier, *in* M.Everaert, T.Lentz, H.de Mulder, O.Nilsen and A.Zondervan, eds, 'The Linguistic Enterprise', *Linguistik Aktuell* 150. Benjamins.
- Nouwen, Rick (2015), Modified numerals: the epistemic effect, *in* L.Alonso-Ovalle and P.Menendez-Benito, eds, 'Epistemic Indefinites: Exploring Modality Beyond the Verbal Domain', Oxford University Press, pp. 244–266.
- Schwarz, Bernhard, Brian Buccola and Michael Hamilton (2012), 'Two types of class b numeral modifiers: A reply to nouwen 2010', *Semantics and Pragmatics* **5**, 1–25.
- Van Tiel, Bob, Emiel Van Miltenburg, Natalia Zevakhina and Bart Geurts (2014), 'Scalar diversity', *Journal of Semantics* p. ffu017.

## Bottom-of-the-scale effect

- ▶ Schwarz et al. (2012) : *Up to* differs from expressions like *at most* and *maximally* in another way: it displays the *bottom-of-the-scale effect*

- (20)
- At most ten people died in the crash.
  - At most one person died in the crash.

## Bottom-of-the-scale effect

- ▶ Schwarz et al. (2012) : *Up to* differs from expressions like *at most* and *maximally* in another way: it displays the *bottom-of-the-scale effect*

- (20)
- At most ten people died in the crash.
  - At most one person died in the crash.

- (21)
- Up to ten people died in the crash.
  - #Up to one person died in the crash.



## Bottom-of-the-scale effect

- ▶ The bounds in combination with the range requirement explain the bottom-of-the-scale effect
- ▶ *All* class B numeral modifiers that set an upper bound require quantification over a range of values and display the bottom-of-the-scale effect as a result

## Bottom-of-the-scale effect

- ▶ The bounds in combination with the range requirement explain the bottom-of-the-scale effect
- ▶ *All* class B numeral modifiers that set an upper bound require quantification over a range of values and display the bottom-of-the-scale effect as a result

(22) a. #Up to one person died in the crash. {p<sub>1</sub>}

## Bottom-of-the-scale effect

- ▶ The bounds in combination with the range requirement explain the bottom-of-the-scale effect
- ▶ *All* class B numeral modifiers that set an upper bound require quantification over a range of values and display the bottom-of-the-scale effect as a result

(22) a. #Up to one person died in the crash.  $\{p_1\}$

(23) a. #At most zero people died in the crash.  $\{p_0\}$

## Bottom-of-the-scale effect

- ▶ The bounds in combination with the range requirement explain the bottom-of-the-scale effect
- ▶ *All* class B numeral modifiers that set an upper bound require quantification over a range of values and display the bottom-of-the-scale effect as a result

- (22) a. #Up to one person died in the crash.  $\{p_1\}$   
b. Up to two people died in the crash.  $\{p_1, p_2\}$
- (23) a. #At most zero people died in the crash.  $\{p_0\}$

## Bottom-of-the-scale effect

- ▶ The bounds in combination with the range requirement explain the bottom-of-the-scale effect
- ▶ *All* class B numeral modifiers that set an upper bound require quantification over a range of values and display the bottom-of-the-scale effect as a result

- (22) a. #Up to one person died in the crash.  $\{p_1\}$   
b. Up to two people died in the crash.  $\{p_1, p_2\}$
- (23) a. #At most zero people died in the crash.  $\{p_0\}$   
b. At most one person died in the crash.  $\{p_0, p_1\}$

## Experiment 1: $n$ & $m$ 's

Item No	$n$	$m_{\text{under}}$	$m_{\text{over}}$
1	3	2	4
2	2	1.5	3
3	96,500	95,000	96,900
4	5.5	4	6
5	4	3	5
6	9	7	10
7	1	.8	1.2
8	43	40	45
9	152,000	150,000	152,700
10	980	950	1,000
11	249,000,000	242,000,000	249,300,000
12	7	5	8

- ▶ Not 100% round  $n$ 's, but small distance between  $n$  &  $m_{\text{over}}$   $\rightsquigarrow$  possible granularity effects
- ▶ Same effects after excluding those items

## Experiment 1: Translated example filler items

### Contradictory fillers ('Bad fillers')

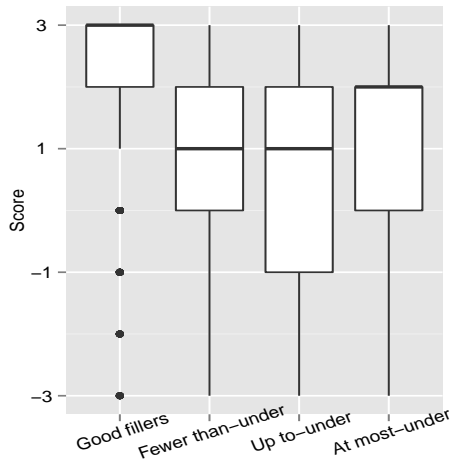
- (24) The Panhellenic examinations started at the end of May; specifically, the examination of the first subject took place on the 10th of June.

### Coherent fillers ('Good fillers')

- (25) Several countries have more than one official language; for example, Belgium has three official languages: Dutch, French and German.

# Experiment 1: Targets vs. Good fillers

## Results

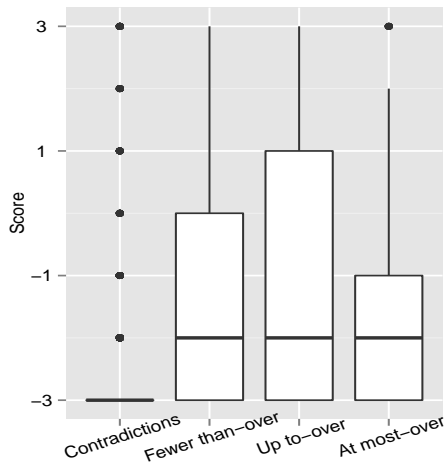


- ▶ Scores for Good fillers significantly higher than scores for 'over' condition for **fewer than** ( $\beta = 1.224$ ,  $SE = .181$ ,  $p < .0001$ ), for **up to** ( $\beta = 1.444$ ,  $SE = .181$ ,  $p < .0001$ ), and for **at most** ( $\beta = 1.18$ ,  $SE = .181$ ,  $p < .0001$ )



# Experiment 1: Targets vs. Bad fillers

## Results



- ▶ Scores for Contradictions significantly lower than scores for 'over' condition for **fewer than** ( $\beta = -1.32$ ,  $SE = .2$ ,  $p < .0001$ ), for **up to** ( $\beta = -1.515$ ,  $SE = .2$ ,  $p < .0001$ ), and for **at most** ( $\beta = -1.244$ ,  $SE = .2$ ,  $p < .0001$ )

## Experiment 2: Example filler items

All = implicature; some = entailment; none = contradiction

CLAIM: The community looked as peaceful as it had through the view point's telescope. *Several* of the houses on the near edge of town were holding yard sales.

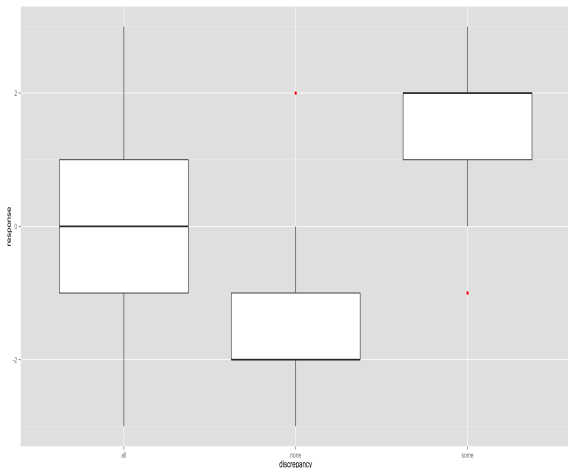
FACT:  $\left\{ \begin{array}{l} \textit{All} \\ \textit{Some} \\ \textit{None} \end{array} \right\}$  of the houses on the near edge of town were holding yard sales.

How compatible is the CLAIM with the FACT?

-3	-2	-1	0	1	2	3
completely incompatible						completely compatible

# Experiment 2: Fillers

## Results

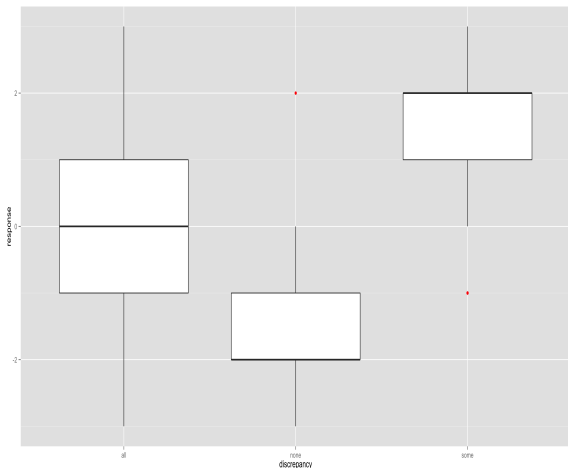


▶ Scores for 'all' (implicature) condition sig. **higher** than scores for 'none' (contradiction) condition ( $\beta = -2.48$ ,  $SE = .338$ ,  $p < .01$ )

▶ Scores for 'all' (implicature) condition sig. **lower** than scores for 'some' (entailment) condition ( $\beta = -2.00$ ,  $SE = .306$ ,  $p < .01$ )

# Experiment 2: Targets vs. fillers

## Results



- ▶ Scores for 'all' (implicature) condition sig. higher than scores for 'over' condition for **at most** ( $\beta = -1.16$ ,  $SE = .286$ ,  $p < .01$ ) and for **fewer than** ( $\beta = -1.52$ ,  $SE = .269$ ,  $p < .01$ ) but not for **up to** ( $\beta = -.05$ ,  $SE = .278$ ,  $p = 0.843$ )
- ▶ Scores for 'some' sig. lower than score for 'under' for each modifier (**fewer than**: ( $\beta = 2.65$ ,  $SE = .357$ ,  $p < .01$ ); **at most**:  $\beta = 1.361$ ,  $SE = .294$ ,  $p < 0.01$ ; **up to**:  $\beta = 1.93$ ,  $SE = .313$ ,  $p < 0.01$ )